

FYJC - MATHEMATICS & STATISTICS

PAPER - I

STRAIGHT LINES

- ❖ if the line makes an angle θ with the positive x – axis then slope of the line is given as

$$m = \tan \theta$$

- ❖ if line passes through points (x_1, y_1) & (x_2, y_2) , then slope of the line is given as

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

- ❖ Given equation of the line : $ax + by + c = 0$; slope is given as

$$m = \frac{-a}{b}$$

- ❖ Slopes of parallel lines are equal : $m_1 = m_2$

- ❖ Product of slopes of perpendicular lines = -1 i.e. $m_1.m_2 = -1$

- ❖ If the line has slope m & passes through point (x_1, y_1) ; then equation of the line can be formed using Slope – Point form

$$y - y_1 = m(x - x_1)$$

- ❖ If the line passes through points (x_1, y_1) & (x_2, y_2) ; then the equation of the line can be formed using Two – Point form

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$$

- ❖ If the line makes x – intercept : a and y – intercept : b on the axes , then the equation of the line can be formed using Double – Intercept form

$$\frac{x}{a} + \frac{y}{b} = 1$$

- ❖ If θ is the acute angle between the two lines having slopes m_1 & m_2 ; then

$$\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right|$$

- ❖ Distance of the line $ax + by + c = 0$ from the origin is given as

$$d = \left| \frac{c}{\sqrt{a^2 + b^2}} \right|$$

- ❖ Distance of the line $ax + by + c = 0$ from the (x_1, y_1) is given as

$$d = \left| \frac{ax_1 + by_1 + c}{\sqrt{a^2 + b^2}} \right|$$

- ❖ Distance between the two parallel lines $ax + by + c_1 = 0$ and $ax + by + c_2 = 0$ is given as

$$d = \left| \frac{c_1 - c_2}{\sqrt{a^2 + b^2}} \right|$$

Q. SET – 1

- 01. find line passing through (2,5) & parallel to $3x - 4y - 7 = 0$
- 02. find line passing through (1,1) and parallel to $4x + y - 11 = 0$
- 03. find line passing through (1,-4) and perpendicular to $x + 2y + 1 = 0$
- 04. find line having x - intercept 4 and parallel to $3x + y + 1 = 0$
- 05. Find equation of the line joining the points (3,-1) and (2,3) . Also find the equation of the line perpendicular to this line and passing through (5,2)
- 06. A(2,1) , B(5,3) and C(-1,3) are vertices of ΔABC . Find equation of
 - a) median through A
 - b) altitude from B
 - c) perpendicular bisector of AC
- 07. Find equation of the line which passes through the point of intersection of the lines $x + 2y - 3 = 0$ and $3x + 4y - 5 = 0$ and which is perpendicular to the line $x - 3y + 5 = 0$

Q. SET – 2

- 01. find equation of the line making equal intercepts on the coordinate axes and passing through (3, -5)
- 02. line makes intercepts of equal magnitude and opposite sign on coordinate axes . If it passes through (-7,2) , find its equation

03. sum of intercepts made by a line on the coordinate axes is 2 . If the line passes through (4, -3) find its equation

04. a line passes through (3,4) and sum of its intercepts made on the coordinate axes is 14 . Find the equation of the line

05. a line passes through (5, -3) and sum of its intercepts made on the coordinate axes is 16 . Find the equation of the line

06. Find equation of the line passing through centroid of triangle ABC whose vertices are A(1,6) , B(-2,9) and C(-2 , 3) such that sum of its intercepts on the coordinate axes is 6 .

07. Find equation of the lines which cut off intercepts on the coordinate axes whose sum is 1 and product is -6

Q SET – 3

01. Find equation of the line passing through (3,5) and the point which bisects the portion of the line $3x + 4y = 24$ intercepted between the coordinate axes

02. Find the equation of line which passes through A(1,2) and the midpoint of the portion of the line $3x - 4y + 24 = 0$ intercepted between the coordinate axes .

03. find equation of the line passing through (-3,1) and the point which divides internally in the ratio 3 : 2 the portion of the line $4x + y = 8$ intercepted between the coordinate axes

Q SET – 4A

01.

find the measure of acute angle between the lines

a) $3x - y + 5 = 0$ & $6x + 3y - 7 = 0$

b) $\sqrt{3}x - y - 4 = 0$ & $x - \sqrt{3}y + 7 = 0$

02.

find the angle subtended by the line segment PQ at the origin if $P(1, \sqrt{3})$ & $Q(\sqrt{3}, 1)$

03.

Show that the line segment joining the points $(\sqrt{3}, 1)$ and $(\sqrt{3}, -1)$ subtends an angle of measure of 60° at the origin

04.

Find equation of a line through origin which makes an angle 45° with the line $6x - 2y + 7 = 0$

05.

find equation of the lines through the point $(3, -5)$ making an angle of 45° with the line $x - 2y + 1 = 0$

06.

Find equations of the lines passing through the point $(4, 5)$ and making an angle of 45° with the line $2x - y + 7 = 0$

07.

find equation of the lines which pass through point $(1, 2)$ and inclined at an angle of 60° to the line $\sqrt{3}x + y - 2 = 0$

08.

find equation of the lines which pass through point $(-1, -4)$ and inclined at an angle of 60° to the line $\sqrt{3}x + y + 5 = 0$

09.

ABC is an equilateral triangle . If $A(1, 2)$ and equation of BC is $x + y + 5 = 0$, find the equation of the sides AB and AC

10.

the base of an equilateral triangle is the line $x + y - 2 = 0$ & the vertex is at the point $(2, -1)$. Find the equation of other sides

11.

if the acute angle between the lines $4x - y + 7 = 0$ and $kx - 5y - 9 = 0$ is 45° , find k

4B

01.

if $(3, -5)$ and $(-1, 3)$ are the opposite vertices of a square , find the equation of the sides

02.

if $(1, 2)$ and $(3, 8)$ are the opposite vertices of a square , find the equation of the sides

Q SET - 5A

01.

Find equation of the line parallel to $3x - 4y - 1 = 0$ and which is at a distance of 3 units from the point $(2, -1)$

02.

Find equation of the line parallel to $3x - 4y - 7 = 0$ and which is at a distance of 4 units from the point $(-2, 1)$

03.

Find equation of the line parallel to $3x + y - 8 = 0$ and which is at a distance of $\sqrt{10}$ units from the point $(3, 1)$

04.

Find equation of the line parallel to $x + 3y - 5 = 0$ and which is at a distance of $3\sqrt{10}$ units from the point $(2, -2)$

Q SET - 5B

01.

Find the points on the line $x + y + 3 = 0$ whose distance from $x + 2y + 2 = 0$ is $\sqrt{5}$ units

ans : $(-9,6)$ and $(1, -4)$

02.

Find the points on the line $x + y - 4 = 0$ whose distance from $4x + 3y = 10$ is 1 unit

ans : $(3,1)$ and $(-7,11)$

03.

Find the points on the line $2x + 3y + 4 = 0$ which are at a distance of 2 units from the line $3x + 4y - 6 = 0$

ans : $(64, -44)$ and $(4, -4)$

04.

Find the points on the line $2x + y - 3 = 0$ whose distance from $6x - 8y - 3 = 0$ is 0.5 units

ans : $(\frac{16}{11}, \frac{1}{11})$; $(1, 1)$

05.

Find the coordinates of the point on X - axis whose distance from the line $x + \sqrt{3}y - 2 = 0$ is 5 units

ans : $(12,0)$ and $(-8,0)$

MISC.

01. The points $A(2,3)$, $B(4, -1)$ and $C(-1,2)$ are the vertices of ΔABC . Find the length of the perpendicular from C on AB and hence find then area of ΔABC

ans : 7 sq. units

02. If the length of perpendicular distance is p units from the origin to the line :

$$\frac{x}{a} + \frac{y}{b} = 1$$

then prove that : $\frac{1}{a^2} + \frac{1}{b^2} = \frac{1}{p^2}$

SOLUTION - QSET 1

01. find line passing through (2,5) and parallel to $3x - 4y - 7 = 0$

$$3x - 4y - 7 = 0$$

$$m = \frac{-a}{b} = -\frac{3}{-4} = \frac{3}{4}$$

Required Line

$$m = 3/4, (// \text{ lines})$$

passing through (2,5)

$$y - y_1 = m(x - x_1)$$

$$y - 5 = \frac{3}{4}(x - 2)$$

$$4y - 20 = 3x - 6$$

$$3x - 4y + 14 = 0$$

02. find line passing through (1,1) and parallel to $4x + y - 11 = 0$

$$4x + y - 11 = 0$$

$$m = \frac{-a}{b} = -\frac{4}{1} = -4$$

Required Line

$$m = -4, (// \text{ lines})$$

passing through (1,1)

$$y - y_1 = m(x - x_1)$$

$$y - 1 = -4(x - 1)$$

$$y - 1 = -4x + 4$$

$$4x + y - 5 = 0$$

03. find line passing through (1,-4) and perpendicular to $x + 2y + 1 = 0$

$$x + 2y + 1 = 0$$

$$m = \frac{-a}{b} = -\frac{1}{2}$$

Required Line

$$m = 2, (\perp \text{ lines})$$

passing through (1,-4)

$$y - y_1 = m(x - x_1)$$

$$y + 4 = 2(x - 1)$$

$$y + 4 = 2x - 2$$

$$2x - y - 6 = 0$$

04. find line having x - intercept 4 and parallel to $3x + y + 1 = 0$

$$3x + y + 1 = 0$$

$$m = \frac{-a}{b} = -\frac{3}{1} = -3$$

Required Line

$$m = -3, (// \text{ lines})$$

passing through (4,0)

$$y - y_1 = m(x - x_1)$$

$$y - 0 = -3(x - 4)$$

$$y - 0 = -3x + 12$$

$$3x + y - 12 = 0$$

05. Find equation of the line joining the points (3,-1) and (2,3). Also find the equation of the line perpendicular to this line and passing through (5,2)

A(3,-1), B(2,3)

Equation of AB

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1}(x - x_1)$$

$$y + 1 = \frac{3 - (-1)}{2 - 3}(x - 3)$$

$$y + 1 = \frac{4}{-1}(x - 3)$$

$$-y - 1 = 4x - 12$$

$$4x + y - 11 = 0 \dots\dots\dots \text{equation of AB}$$

let PQ \perp AB

$$m_{AB} = -4 \therefore m_{PQ} = \frac{1}{4}$$

Equation of PQ

$$m = 1/4, (5,2)$$

$$y - y_1 = m(x - x_1)$$

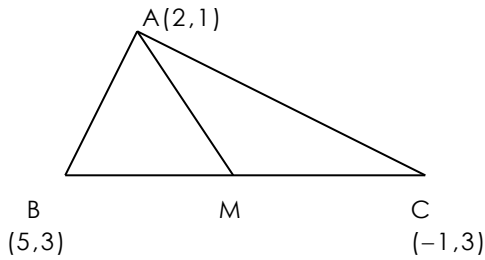
$$y - 2 = \frac{1}{4}(x - 5)$$

$$4y - 8 = x - 5$$

$$x - 4y + 3 = 0$$

06. A(2,1) , B(5,3) and C(-1,3) are vertices of ΔABC . Find equation of

a) median through A (say AM)



$$M \equiv \left(\frac{5-1}{2}, \frac{3+3}{2} \right) \equiv (2, 3)$$

equation of median AM

A(2,1) , B(2,3)

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$$

$$y + 1 = \frac{3 - 1}{2 - 2} (x - 2)$$

$$0 = 2x - 4$$

$$x = 2$$

c) perpendicular Bisector of AC (say PQ)

$$m_{AC} = \frac{3-1}{-1-2} = -\frac{2}{3}$$

$$m_{PQ} = \frac{3}{2} \quad (PQ \perp AC)$$

$$\text{midpoint of AC} \equiv \left(\frac{2-1}{2}, \frac{1+3}{2} \right)$$

$$\equiv \left(\frac{1}{2}, 2 \right)$$

Equation of PQ

$$m = \frac{3}{2}, \left(\frac{1}{2}, 2 \right)$$

$$y - y_1 = m (x - x_1)$$

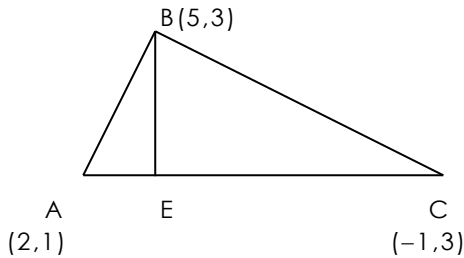
$$y - 2 = \frac{3}{2} \left(x - \frac{1}{2} \right)$$

$$y - 2 = \frac{3}{4} (2x - 1)$$

$$4y - 8 = 6x - 3$$

$$6x - 4y + 5 = 0$$

b) altitude through B (say BE)



$$m_{AC} = \frac{3-1}{-1-2} = -\frac{2}{3}$$

$$m_{BE} = \frac{3}{2} \quad (BE \perp AC)$$

Equation of BE

$$m = \frac{3}{2}, (5,3)$$

$$y - y_1 = m (x - x_1)$$

$$y - 3 = \frac{3}{2} (x - 5)$$

$$2y - 6 = 3x - 15$$

$$3x - 2y - 9 = 0$$

07. Find equation of the line which passes through the point of intersection of the lines $x + 2y - 3 = 0$ and $3x + 4y - 5 = 0$ and which is perpendicular to the line $x - 3y + 5 = 0$

Point of Intersection

$$x + 2y = 3 \quad \times 2$$

$$3x + 4y = 5$$

$$3x + 4y = 5$$

$$\underline{2x + 4y = 6}$$

$$x = -1$$

subs in (1) $y = 2 \quad \therefore (-1, 2)$

slope of line $x - 3y + 5 = 0$

$$m = \frac{-a}{b} = \frac{-1}{-3} = \frac{1}{3}$$

slope of required line = -3 (\perp lines)

Equation of required line

$m = -3$, passing through $(-1, 2)$

$$y - y_1 = m(x - x_1)$$

$$y - 2 = -3(x + 1)$$

$$y - 2 = -3x - 3$$

$$3x + y + 1 = 0$$

SOLUTION - QSET 2

01. find equation of the line making equal intercepts on the coordinate axes and passing through (3, -5)

$$a = b \text{ given}$$

let the equation of the line be

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{a} + \frac{y}{a} = 1$$

$$x + y = a$$

since the line passes through (3,-5) , it must satisfy the equation

$$3 - 5 = a$$

$$a = -2$$

Hence the equation is

$$x + y = -2$$

$$\underline{x + y + 2 = 0}$$

02. line makes intercepts of equal magnitude and opposite sign on coordinate axes . If it passes through (-7,2) , find its equation

$$a = -b \text{ given}$$

let the equation of the line be

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{a} + \frac{y}{-a} = 1$$

$$x - y = a$$

since the line passes through (-7,2) , it must satisfy the equation

$$-7 - 2 = a$$

$$a = -9$$

Hence the equation is

$$x - y = -9$$

$$\underline{x - y + 9 = 0}$$

03. sum of intercepts made by a line on the coordinate axes is 2 . If the line passes through (4, -3) find its equation .

$$a + b = 2 \text{ given}$$

$$b = 2 - a \text{ (1)}$$

let the equation of the line be

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{a} + \frac{y}{2-a} = 1$$

since the line passes through (4,-3) , it must satisfy the equation

$$\frac{4}{a} + \frac{-3}{2-a} = 1$$

$$8 - 4a - 3a = a(2 - a)$$

$$8 - 7a = 2a - a^2$$

$$a^2 - 9a + 8 = 0$$

$$a^2 - 8a - 1a + 8 = 0$$

$$a(a - 8) - 1(a - 8) = 0$$

$$(a - 8)(a - 1) = 0$$

$$a = 8$$

$$b = 2 - a$$

$$= 2 - 8$$

$$= -6$$

Equation

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{8} + \frac{y}{-6} = 1$$

$$\frac{x}{8} - \frac{y}{6} = 1$$

$$6x - 8y = 48$$

$$\underline{3x - 4y = 24}$$

$$a = 1$$

$$b = 2 - a$$

$$= 2 - 1$$

$$= 1$$

Equation

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{1} + \frac{y}{1} = 1$$

$$\underline{x + y = 1}$$

04. a line passes through (3,4) and sum of its intercepts made on the coordinate axes is 14 . Find the equation of the line

$$a + b = 14 \quad \text{..... given}$$

$$b = 14 - a \quad \text{..... (1)}$$

let the equation of the line be

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{a} + \frac{y}{14 - a} = 1$$

since the line passes through (3,4) , it must satisfy the equation

$$\frac{3}{a} + \frac{4}{14 - a} = 1$$

$$42 - 3a + 4a = a(14 - a)$$

$$42 + a = 14a - a^2$$

$$a^2 - 13a + 42 = 0$$

$$a^2 - 6a - 7a + 80 = 0$$

$$a(a - 6) - 7(a - 20) = 0$$

$$(a - 6)(a - 7) = 0$$

$$a = 6$$

$$b = 14 - a$$

$$= 14 - 6$$

$$= 8$$

Equation

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{6} + \frac{y}{8} = 1$$

$$\frac{8x + 6y}{48} = 1$$

$$8x + 6y = 48$$

$$\underline{4x + 3y = 24}$$

$$a = 7$$

$$b = 14 - a$$

$$= 14 - 7$$

$$= 7$$

Equation

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{7} + \frac{y}{7} = 1$$

$$\underline{x + y = 7}$$

05. a line passes through (5, -3) and sum of its intercepts made on the coordinate axes is 16 . Find the equation of the line

$$a + b = 16 \quad \text{..... given}$$

$$b = 16 - a \quad \text{..... (1)}$$

let the equation of the line be

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{a} + \frac{y}{16 - a} = 1$$

since the line passes through (5,-3) , it must satisfy the equation

$$\frac{5}{a} + \frac{-3}{16 - a} = 1$$

$$80 - 5a - 3a = a(16 - a)$$

$$80 - 8a = 16a - a^2$$

$$a^2 - 24a + 80 = 0$$

$$a^2 - 20a - 4a + 80 = 0$$

$$a(a - 20) - 4(a - 20) = 0$$

$$(a - 20)(a - 4) = 0$$

$$a = 4$$

$$b = 16 - a$$

$$= 16 - 4$$

$$= 12$$

Equation

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{4} + \frac{y}{12} = 1$$

$$\frac{3x + y}{12} = 1$$

$$3x + y = 12$$

$$\underline{3x + y - 12 = 0}$$

$$a = 20$$

$$b = 16 - a$$

$$= 16 - 20$$

$$= -4$$

Equation

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{20} + \frac{y}{-4} = 1$$

$$\frac{x - y}{20} = 1$$

$$\frac{x - 5y}{20} = 1$$

$$\underline{x - 5y = 20}$$

06. Find equation of the line passing through centroid of triangle ABC whose vertices are A(1,6) , B(-2,9) and C(-2 , 3) such that sum of its intercepts on the coordinate axes is 6 .

$$G \equiv \left(\frac{1-2-2}{3}, \frac{6+9+3}{3} \right) \equiv (-1, 6)$$

$a + b = 6$ given

$b = 6 - a$ (1)

let the equation of the line be

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{a} + \frac{y}{6-a} = 1$$

since the line passes through (-1,6) , it must satisfy the equation

$$\frac{-1}{a} + \frac{6}{6-a} = 1$$

$$-6 + a + 6a = a(6 - a)$$

$$-6 + 7a = 6a - a^2$$

$$a^2 + a - 6 = 0$$

$$a^2 + 3a - 2a - 6 = 0$$

$$(a + 3)(a - 2) = 0$$

$a = -3$

$b = 6 - a$

$= 6 + 3$

$= 9$

Equation

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{-3} + \frac{y}{9} = 1$$

$$9x - 3y = -27$$

$$\underline{3x - y + 9 = 0}$$

$a = 2$

$b = 6 - a$

$= 6 - 2$

$= 4$

Equation

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{2} + \frac{y}{4} = 1$$

$$\frac{2x + y}{4} = 1$$

$$\underline{2x + y = 4}$$

07. Find equation of the lines which cut off intercepts on the coordinate axes whose sum is 1 and product is -6

$a + b = 1 \therefore b = 1 - a$

$ab = -6$

$a(1 - a) = -6$

$a - a^2 = -6$

$a^2 - a - 6 = 0$

$a^2 - 3a + 2a - 6 = 0$

$a(a - 3) + 2(a - 3) = 0$

$(a - 3)(a + 2) = 0$

$a = 3$

$b = 1 - a$

$= 1 - 3$

$= -2$

Equation

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{3} + \frac{y}{-2} = 1$$

$$-2x + 3y = -6$$

$$\underline{2x - 3y - 6 = 0}$$

$a = -2$

$b = 1 - a$

$= 1 + 2$

$= 3$

Equation

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$\frac{x}{-2} + \frac{y}{3} = 1$$

$$\frac{3x - 2y}{-6} = 1$$

$$3x - 2y = -6$$

$$\underline{3x - 2y + 6 = 0}$$

SOLUTION - QSET 3

01.

Find equation of the line passing through (3,5) and the point which bisects the portion of the line $3x + 4y = 24$ intercepted between the coordinate axes

SOLUTION

STEP 1 :

$$3x + 4y = 24$$

$$\text{put } y = 0 \quad ; \quad x = 8 \quad \therefore A (8,0)$$

$$\text{put } x = 0 \quad ; \quad y = 6 \quad \therefore B (0,6)$$

STEP 2 :

P is the midpoint of AB

Using midpoint formula

$$P \equiv \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$\equiv \left(\frac{8+0}{2}, \frac{0+6}{2} \right)$$

$$P \equiv (4,3)$$

STEP 3 :

Line is passing through (3,5) & (4,3)

Equation of the line

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$$

$$y - 5 = \frac{3 - 5}{4 - 3} (x - 3)$$

$$y - 5 = -2(x - 3)$$

$$y - 5 = -2x + 6$$

$$2x + y - 5 - 6 = 0$$

$$2x + y - 11 = 0$$

02.

Find the equation of line which passes through A(1,2) and the midpoint of the portion of the line $3x - 4y + 24 = 0$ intercepted between the coordinate axes .

SOLUTION

STEP 1 :

$$3x - 4y + 24 = 0$$

$$\text{put } y = 0 \quad ; \quad 3x + 24 = 0$$

$$3x = -24 \quad \therefore P (-8,0)$$

$$\text{put } x = 0 \quad ; \quad -4y + 24 = 0$$

$$-4y = -24 \quad \therefore Q (0,6)$$

STEP 2 :

Let B be the midpoint of PQ

Using midpoint formula

$$B \equiv \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$\equiv \left(\frac{-8+0}{2}, \frac{0+6}{2} \right)$$

$$B \equiv (-4,3)$$

STEP 3 :

Line is passing through (1,2) & (-4,3)

Equation of the line

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$$

$$y - 2 = \frac{3 - 2}{-4 - 1} (x - 1)$$

$$y - 2 = \frac{1}{-5} (x - 1)$$

$$-5y + 10 = x - 1$$

$$x + 5y - 11 = 0$$

03.

find equation of the line passing through (-3,1) and the point which divides internally in the ratio 3 : 2 the portion of the line $4x + y = 8$ intercepted between the coordinate axes

SOLUTION

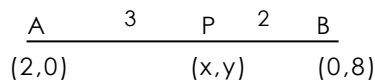
STEP 1 :

$$4x + y = 8$$

$$\text{put } y = 0 \quad ; \quad x = 2 \quad \therefore A (2,0)$$

$$\text{put } x = 0 \quad ; \quad y = 8 \quad \therefore B (0,8)$$

STEP 2 :



P divides seg AB internally in the ratio 3:2

Using section formula

$$P \equiv \left(\frac{mx_2 + nx_1}{2}, \frac{my_2 + ny_1}{2} \right)$$

$$\equiv \left(\frac{3(0) + 2(2)}{3 + 2}, \frac{3(8) + 2(0)}{3 + 2} \right)$$

$$P \equiv (4/5, 24/5)$$

STEP 3 :

Line is passing through (-3,1) & (4/5,24/5)

Equation of the line

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$$

$$y - 1 = \frac{24 - 1}{\frac{4}{5} + 3} (x + 3)$$

$$\frac{4 + 3}{5}$$

$$y - 1 = \frac{19}{5} (x + 3)$$

$$\frac{19}{5}$$

$$y - 1 = x + 3$$

$$x - y + 4 = 0$$

SOLUTION - QSET 4

01.

find the measure of acute angle between the lines

$$a) 3x - y + 5 = 0 \text{ \& } 6x + 3y - 7 = 0$$

$$3x - y + 5 = 0 \quad ; \quad m_1 = -\frac{a}{b} = -\frac{3}{-1} = 3$$

$$6x + 3y - 7 = 0; \quad m_2 = -\frac{a}{b} = -\frac{6}{3} = -2$$

$$\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1.m_2} \right|$$

$$= \left| \frac{3 - (-2)}{1 + 3(-2)} \right|$$

$$= \left| \frac{5}{-5} \right|$$

$$= 1$$

$$\theta = 45^\circ$$

$$b) \sqrt{3}x - y - 4 = 0 \text{ \& } x - \sqrt{3}y + 7 = 0$$

$$\sqrt{3}x - y - 4 = 0; \quad m_1 = -\frac{a}{b} = -\frac{\sqrt{3}}{-1} = \sqrt{3}$$

$$x - \sqrt{3}y + 7 = 0; \quad m_2 = -\frac{a}{b} = -\frac{1}{-\sqrt{3}} = \frac{1}{\sqrt{3}}$$

$$\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1.m_2} \right|$$

$$= \left| \frac{\sqrt{3} - \frac{1}{\sqrt{3}}}{1 + \sqrt{3} \cdot \frac{1}{\sqrt{3}}} \right|$$

$$= \left| \frac{\frac{3 - 1}{\sqrt{3}}}{1 + 1} \right|$$

$$= \frac{1}{\sqrt{3}}$$

$$\theta = 30^\circ$$

02.

find the angle subtended by the line segment PQ at the origin if P(1,√3) & Q(√3,1)

SOLUTION

$$OP : m_1 = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\sqrt{3} - 0}{1 - 0} = \sqrt{3}$$

$$OQ : m_2 = \frac{y_2 - y_1}{x_2 - x_1} = \frac{1 - 0}{\sqrt{3} - 0} = \frac{1}{\sqrt{3}}$$

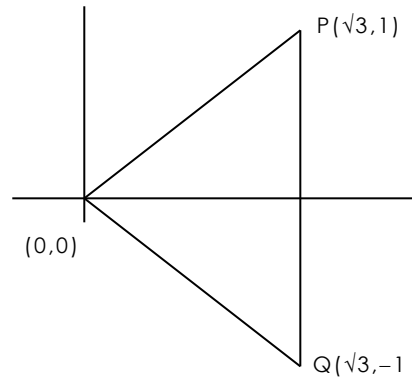
let θ be the angle subtended by PQ at the origin (θ is the angle between the lines OP & OQ)

$$\begin{aligned} \tan \theta &= \left| \frac{m_1 - m_2}{1 + m_1.m_2} \right| \\ &= \left| \frac{\sqrt{3} - \frac{1}{\sqrt{3}}}{1 + \sqrt{3} \cdot \frac{1}{\sqrt{3}}} \right| \\ &= \left| \frac{\frac{3 - 1}{\sqrt{3}}}{1 + 1} \right| \\ &= \frac{1}{\sqrt{3}} \end{aligned}$$

$$\theta = 30^\circ$$

03.

Show that the line segment joining the points (√3,1) and (√3,-1) subtends an angle of measure of 60° at the origin



SOLUTION

Let P(√3,1) and Q(√3,-1)

$$OP : m_1 = \frac{y_2 - y_1}{x_2 - x_1} = \frac{1 - 0}{\sqrt{3} - 0} = \frac{1}{\sqrt{3}}$$

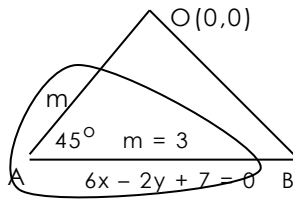
$$OQ : m_2 = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-1 - 0}{\sqrt{3} - 0} = -\frac{1}{\sqrt{3}}$$

let θ be the angle subtended by PQ at the origin (θ is the angle between the lines OP & OQ)

$$\begin{aligned} \tan \theta &= \left| \frac{m_1 - m_2}{1 + m_1.m_2} \right| \\ &= \left| \frac{\frac{1}{\sqrt{3}} + \frac{1}{\sqrt{3}}}{1 + \frac{1}{\sqrt{3}} \cdot \frac{-1}{\sqrt{3}}} \right| \\ &= \left| \frac{\frac{2}{\sqrt{3}}}{1 - \frac{1}{3}} \right| \\ &= \left| \frac{\frac{2}{\sqrt{3}}}{\frac{2}{3}} \right| \\ &= \frac{3}{\sqrt{3}} \\ &= \sqrt{3} \\ \theta &= 60^\circ \end{aligned}$$

04.

Find equation of a line through origin which makes an angle 45° with the line $6x - 2y + 7 = 0$



STEP 1 :

$$6x - 2y + 7 = 0$$

$$m = \frac{-a}{b} = \frac{-6}{(-2)} = 3$$

STEP 2 :

$$\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1.m_2} \right|$$

$$\tan 45 = \left| \frac{m - 3}{1 + m(3)} \right|$$

$$1 = \left| \frac{m - 3}{1 + 3m} \right|$$

$$\begin{array}{l|l} \frac{m - 3}{1 + 3m} = 1 & \frac{m - 3}{1 + 3m} = -1 \\ m - 3 = 1 + 3m & m - 3 = -1 - 3m \\ m - 3m = 1 + 3 & m + 3m = -1 + 3 \\ -2m = 4 & 4m = 2 \\ m = -2 & m = \frac{1}{2} \end{array}$$

STEP 3

Equation of OA : $m = -2$, $O(0,0)$

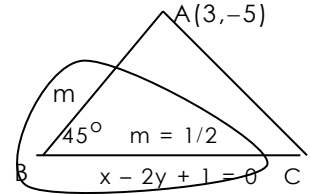
$$\begin{aligned} y - y_1 &= m(x - x_1) \\ y - 0 &= -2(x - 0) \\ y &= -2x \\ 2x + y &= 0 \end{aligned}$$

Equation of OB : $m = \frac{1}{2}$, $O(0,0)$

$$\begin{aligned} y - y_1 &= m(x - x_1) \\ y - 0 &= \frac{1}{2}(x - 0) \\ 2y &= x \\ x - 2y &= 0 \end{aligned}$$

05.

find equation of the lines through the point $(3, -5)$ making an angle of 45° with the line $x - 2y + 1 = 0$



STEP 1 :

$$x - 2y + 1 = 0$$

$$m = \frac{-a}{b} = \frac{-1}{(-2)} = \frac{1}{2}$$

STEP 2 :

$$\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1.m_2} \right|$$

$$\tan 45 = \left| \frac{m - 1/2}{1 + m(1/2)} \right|$$

$$1 = \left| \frac{2m - 1}{2 + m} \right|$$

$$\begin{array}{l|l} \frac{2m - 1}{2 + m} = 1 & \frac{2m - 1}{2 + m} = -1 \\ 2m - 1 = 2 + m & 2m - 1 = -2 - m \\ 2m - m = 2 + 1 & 2m + m = -2 + 1 \\ m = 3 & 3m = -1 \\ m = 3 & m = \frac{-1}{3} \end{array}$$

STEP 3

Equation of AB : $m = 3$, $A(3,-5)$

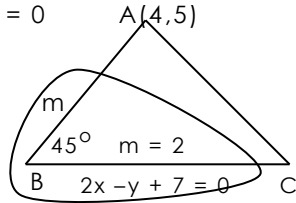
$$\begin{aligned} y - y_1 &= m(x - x_1) \\ y + 5 &= 3(x - 3) \\ y + 5 &= 3x - 9 \\ 3x - y - 14 &= 0 \end{aligned}$$

Equation of AC : $m = \frac{-1}{3}$, $A(3,-5)$

$$\begin{aligned} y - y_1 &= m(x - x_1) \\ y + 5 &= \frac{-1}{3}(x - 3) \\ 3y + 15 &= -x + 3 \\ x + 3y + 12 &= 0 \end{aligned}$$

06.

Find equations of the lines passing through the point (4,5) and making an angle of 45° with the line $2x - y + 7 = 0$



STEP 1 :

$$2x - y + 7 = 0$$

$$m = \frac{-a}{b} = \frac{-2}{(-1)} = 2$$

STEP 2 :

$$\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right|$$

$$\tan 45 = \left| \frac{m - 2}{1 + m(2)} \right|$$

$$1 = \left| \frac{m - 2}{1 + 2m} \right|$$

$\frac{m - 2}{1 + 2m} = 1$	$\frac{m - 2}{1 + 2m} = -1$
$m - 2 = 1 + 2m$	$m - 2 = -1 - 2m$
$m - 2m = 1 + 2$	$m + 2m = -1 + 2$
$-m = 3$	$3m = 2$
$m = -3$	$m = \frac{2}{3}$

STEP 3

Equation of AB : $m = -3$, A(4, 5)

$$y - y_1 = m(x - x_1)$$

$$y - 5 = -3(x - 4)$$

$$y - 5 = -3x + 12$$

$$3x + y - 17 = 0$$

Equation of AC : $m = \frac{1}{3}$, A(4, 5)

$$y - y_1 = m(x - x_1)$$

$$y - 5 = \frac{1}{3}(x - 4)$$

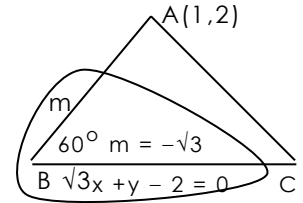
$$3y - 15 = x - 4$$

$$x - 3y + 15 - 4 = 0$$

$$x - 3y + 11 = 0$$

07.

find equation of the lines which pass through point (1,2) and inclined at an angle of 60° to the line $\sqrt{3}x + y - 2 = 0$



STEP 1 :

$$\sqrt{3}x + y - 2 = 0$$

$$m = \frac{-a}{b} = \frac{-\sqrt{3}}{1} = -\sqrt{3}$$

STEP 2 :

$$\tan \theta = \frac{m_1 - m_2}{1 + m_1 m_2}$$

$$\tan 60 = \left| \frac{m + \sqrt{3}}{1 + m(-\sqrt{3})} \right|$$

$$\sqrt{3} = \left| \frac{m + \sqrt{3}}{1 - \sqrt{3}m} \right|$$

$\frac{m + \sqrt{3}}{1 - \sqrt{3}m} = \sqrt{3}$	$\frac{m + \sqrt{3}}{1 - \sqrt{3}m} = -\sqrt{3}$
$m + \sqrt{3} = \sqrt{3} - 3m$	$m + \sqrt{3} = -\sqrt{3} + 3m$
$m + 3m = \sqrt{3} - \sqrt{3}$	$m - 3m = -\sqrt{3} - \sqrt{3}$
$4m = 0$	$-2m = -2\sqrt{3}$
$m = 0$	$m = \sqrt{3}$

STEP 3

Equation of AB : $m = 0$, A(1, 2)

$$y - y_1 = m(x - x_1)$$

$$y - 2 = 0(x - 1)$$

$$y - 2 = 0$$

Equation of AC : $m = \sqrt{3}$, A(1, 2)

$$y - y_1 = m(x - x_1)$$

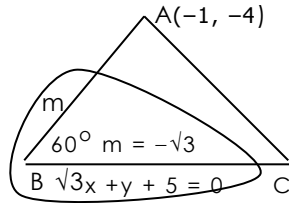
$$y - 2 = \sqrt{3}(x - 1)$$

$$y - 2 = \sqrt{3}x - \sqrt{3}$$

$$\sqrt{3}x - y + 2 - \sqrt{3} = 0$$

08.

find equation of the lines which pass through point $(-1, -4)$ and inclined at an angle of 60° to the line $\sqrt{3}x + y + 5 = 0$



STEP 1 :

$$\sqrt{3}x + y + 5 = 0$$

$$m = \frac{-a}{b} = \frac{-\sqrt{3}}{1} = -\sqrt{3}$$

STEP 2 :

$$\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1.m_2} \right|$$

$$\tan 60 = \left| \frac{m + \sqrt{3}}{1 + m(-\sqrt{3})} \right|$$

$$\sqrt{3} = \left| \frac{m + \sqrt{3}}{1 - \sqrt{3}m} \right|$$

$\frac{m + \sqrt{3}}{1 - \sqrt{3}m} = \sqrt{3}$	$\frac{m + \sqrt{3}}{1 - \sqrt{3}m} = -\sqrt{3}$
$m + \sqrt{3} = \sqrt{3} - 3m$	$m + \sqrt{3} = -\sqrt{3} + 3m$
$m + 3m = \sqrt{3} - \sqrt{3}$	$m - 3m = -\sqrt{3} - \sqrt{3}$
$4m = 0$	$-2m = -2\sqrt{3}$
$m = 0$	$m = \sqrt{3}$

STEP 3

Equation of AB : $m = 0$, $A(-1, -4)$

$$y - y_1 = m(x - x_1)$$

$$y + 4 = 0(x + 1)$$

$$y + 4 = 0$$

Equation of AC : $m = \sqrt{3}$, $A(-1, -4)$

$$y - y_1 = m(x - x_1)$$

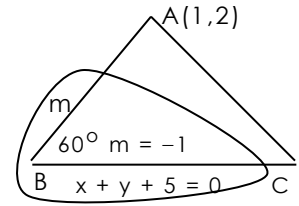
$$y + 4 = \sqrt{3}(x + 1)$$

$$y + 4 = \sqrt{3}x + \sqrt{3}$$

$$\sqrt{3}x - y + \sqrt{3} - 4 = 0$$

09.

ABC is an equilateral triangle . If $A(1,2)$ and equation of BC is $x + y + 5 = 0$, find the equation of the sides AB and AC



STEP 1 :

$$x + y + 5 = 0$$

$$m = \frac{-a}{b} = \frac{-1}{1} = -1$$

STEP 2 :

$$\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1.m_2} \right|$$

$$\tan 60 = \left| \frac{m + 1}{1 + m(-1)} \right|$$

$$\sqrt{3} = \left| \frac{m + 1}{1 - m} \right|$$

$\frac{m + 1}{1 - m} = \sqrt{3}$	$\frac{m + 1}{1 - m} = -\sqrt{3}$
$m + 1 = \sqrt{3} - \sqrt{3}m$	$m + 1 = -\sqrt{3} + \sqrt{3}m$
$m + \sqrt{3}m = \sqrt{3} - 1$	$1 + \sqrt{3} = \sqrt{3}m - m$
$m(1 + \sqrt{3}) = \sqrt{3} - 1$	$1 + \sqrt{3} = m(\sqrt{3} - 1)$
$m = \frac{\sqrt{3} - 1}{\sqrt{3} + 1}$	$m = \frac{\sqrt{3} + 1}{\sqrt{3} - 1}$

$m = \frac{\sqrt{3} - 1}{\sqrt{3} + 1} \cdot \frac{\sqrt{3} - 1}{\sqrt{3} - 1}$	$m = \frac{\sqrt{3} + 1}{\sqrt{3} - 1} \cdot \frac{\sqrt{3} + 1}{\sqrt{3} + 1}$
---	---

$$= \frac{(\sqrt{3} - 1)^2}{3 - 1}$$

$$= \frac{(\sqrt{3} + 1)^2}{3 - 1}$$

$$= \frac{3 - 2\sqrt{3} + 1}{2}$$

$$= \frac{3 + 2\sqrt{3} + 1}{2}$$

$$= \frac{4 - 2\sqrt{3}}{2}$$

$$= \frac{4 + 2\sqrt{3}}{2}$$

$$= 2 - \sqrt{3}$$

$$= 2 + \sqrt{3}$$

STEP 3

Equation of AB : $m = 2 - \sqrt{3}$, A(1,2)

$$y - y_1 = m(x - x_1)$$

$$y - 2 = (2 - \sqrt{3})(x - 1)$$

Equation of AC : $m = 2 + \sqrt{3}$, A(1,2)

$$y - y_1 = m(x - x_1)$$

$$y - 2 = (2 + \sqrt{3})(x - 1)$$

10.

the base of an equilateral triangle is the line $x + y - 2 = 0$ & the vertex is at the point (2, -1).

Find the equation of other sides

ans : $y + 1 = (2 - \sqrt{3})(x - 2)$ and

$$y + 1 = (2 + \sqrt{3})(x - 2) \quad \text{REFER SOLN 9}$$

11.

if the acute angle between the lines $4x - y + 7 = 0$ and $kx - 5y - 9 = 0$ is 45° , find k

$$4x - y + 7 = 0 ; \quad m_1 = -\frac{a}{b} = -\frac{4}{-1} = 4$$

$$kx - 5y - 9 = 0 ; \quad m_2 = -\frac{a}{b} = -\frac{k}{-5} = \frac{k}{5}$$

$$\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1.m_2} \right|$$

$$\tan 45 = \left| \frac{4 - \frac{k}{5}}{1 + \frac{4k}{5}} \right|$$

$$1 = \left| \frac{20 - k}{5 + 4k} \right|$$

$$\frac{20 - k}{5 + 4k} = 1$$

$$20 - k = 5 + 4k$$

$$15 = 5k$$

$$k = 3$$

$$\frac{20 - k}{5 + 4k} = -1$$

$$20 - k = -5 - 4k$$

$$3k = -25$$

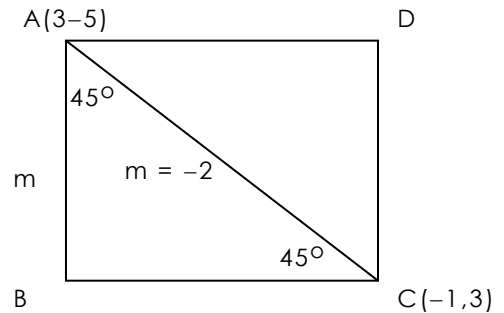
$$k = -25/3$$

3B

01.

if (3, -5) and (-1,3) are the opposite vertices of a square , find the equation of the sides

SOLUTION :



STEP 1 :

A(3,-5) , C(-1, 3)

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{3 + 5}{-1 - 3} = -2$$

STEP 2 :

$$\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1.m_2} \right|$$

$$\tan 45 = \left| \frac{m + 2}{1 + m(-2)} \right|$$

$$1 = \left| \frac{m + 2}{1 - 2m} \right|$$

$$\frac{m + 2}{1 - 2m} = 1$$

$$m + 2 = 1 - 2m$$

$$m + 2m = 1 - 2$$

$$3m = -1$$

$$m = \frac{-1}{3}$$

let

$$m_{AB} = m_{CD} = \frac{-1}{3}$$

(AB // CD)

$$\frac{m + 2}{1 - 2m} = -1$$

$$m + 2 = -1 + 2m$$

$$m - 2m = -1 - 2$$

$$-m = -3$$

$$m = 3$$

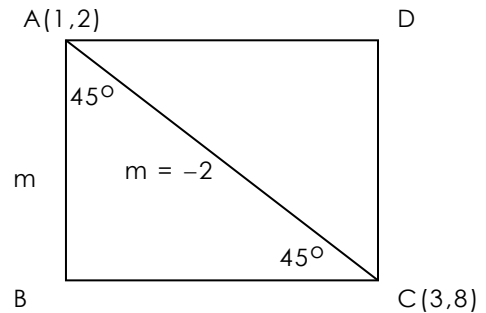
$$m_{BC} = m_{AD} = 3$$

(BC // AD)

02.

if (1, 2) and (3, 8) are the opposite vertices of a square, find the equation of the sides

SOLUTION :



STEP 3 :

Equation of AB : $m = \frac{-1}{3}$, A(3-5)

$$y - y_1 = m(x - x_1)$$

$$y + 5 = \frac{-1}{3}(x - 3)$$

$$3y + 15 = -x + 3$$

$$x + 3y + 12 = 0$$

Equation of BC : $m = 3$, C(-1,3)

$$y - y_1 = m(x - x_1)$$

$$y - 3 = 3(x + 1)$$

$$y - 3 = 3x + 3$$

$$3x - y - 6 = 0$$

Equation of CD : $m = \frac{-1}{3}$, C(-1,3)

$$y - y_1 = m(x - x_1)$$

$$y - 3 = \frac{-1}{3}(x + 1)$$

$$3y - 9 = -x - 1$$

$$x + 3y - 9 + 1 = 0$$

$$x + 3y - 8 = 0$$

Equation of AD : $m = 3$, A(3-5)

$$y - y_1 = m(x - x_1)$$

$$y + 5 = 3(x - 3)$$

$$y + 5 = 3x - 9$$

$$3x - y - 14 = 0$$

STEP 1 :

A(1,2), C(3, 8)

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{8 - 2}{3 - 1} = 3$$

STEP 2 :

$$\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1 \cdot m_2} \right|$$

$$\tan 45 = \left| \frac{m - 3}{1 + m(3)} \right|$$

$$1 = \left| \frac{m - 3}{1 + 3m} \right|$$

$$\frac{m - 3}{1 + 3m} = 1$$

$$m - 3 = 1 + 3m$$

$$m - 3m = 1 + 3$$

$$-2m = 4$$

$$m = -2$$

let

$$m_{AB} = m_{CD} = -2$$

(AB // CD)

$$\frac{m - 3}{1 + 3m} = -1$$

$$m - 3 = -1 - 3m$$

$$m + 3m = -1 + 3$$

$$4m = 2$$

$$m = \frac{1}{2}$$

$$m_{BC} = m_{AD} = \frac{1}{2}$$

(BC // AD)

STEP 3

Equation of AB : $m = -2$, A(1,2)

$$y - y_1 = m(x - x_1)$$

$$y - 2 = -2(x - 1)$$

$$y - 2 = -2x + 2$$

$$2x + y - 4 = 0$$

Equation of BC : $m = \frac{1}{2}$, C(3,8)

$$y - y_1 = m(x - x_1)$$

$$y - 8 = \frac{1}{2}(x - 3)$$

$$2y - 16 = x - 3$$

$$x - 2y + 13 = 0$$

Equation of CD : $m = -2$, C(3,8)

$$y - y_1 = m(x - x_1)$$

$$y - 8 = -2(x - 3)$$

$$y - 8 = -2x + 6$$

$$2x + y - 14 = 0$$

Equation of AD : $m = \frac{1}{2}$, C(1,2)

$$y - y_1 = m(x - x_1)$$

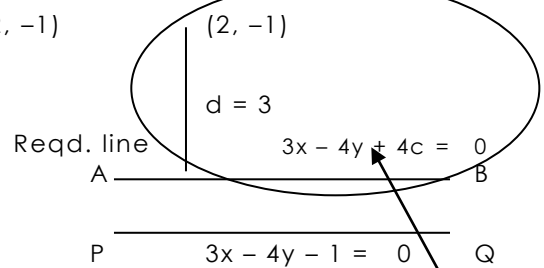
$$y - 2 = \frac{1}{2}(x - 1)$$

$$2y - 4 = x - 1$$

$$x - 2y + 3 = 0$$

01.

Find equation of line parallel to $3x - 4y - 1 = 0$ and which is at a distance of 3 units from the point (2, -1)



STEP 1 : PQ

$$3x - 4y - 1 = 0 \quad m = \frac{-a}{b} = \frac{-3}{-4} = \frac{3}{4}$$

STEP 2 : AB

$$m_{AB} = \frac{3}{4} \quad (AB \parallel PQ)$$

equation of AB : $y = mx + c$

$$y = \frac{3x}{4} + c$$

$$y = \frac{3x + 4c}{4}$$

$$4y = 3x + 4c$$

$$3x - 4y + 4c = 0$$

STEP 3 :

$$d = 3$$

$$\left| \frac{3(2) - 4(-1) + 4c}{\sqrt{3^2 + 4^2}} \right| = 3$$

$$\left| \frac{6 + 4 + 4c}{5} \right| = 3$$

$$\left| \frac{10 + 4c}{5} \right| = 3$$

$$\frac{10 + 4c}{5} = \pm 3$$

$$10 + 4c = \pm 15$$

$$10 + 4c = 15 \quad \left| \quad 10 + 4c = -15 \right.$$

$$4c = 5 \quad \left| \quad 4c = -25 \right.$$

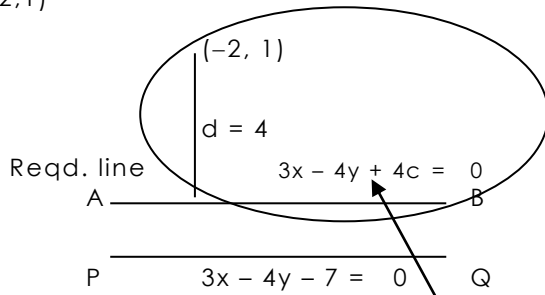
Equation of AB Equation of AB

$$3x - 4y + 5 = 0 \quad \left| \quad 3x - 4y - 25 = 0 \right.$$

SOLUTION - QSET 5A

02.

Find equation of line parallel to $3x - 4y - 7 = 0$ and which is at a distance of 4 units from the point $(-2, 1)$



STEP 1 : PQ

$$3x - 4y - 7 = 0 \quad m = \frac{-a}{b} = \frac{-3}{-4} = \frac{3}{4}$$

STEP 2 : AB

$$m_{AB} = \frac{3}{4} \quad (AB \parallel PQ)$$

$$\text{equation of AB : } y = mx + c$$

$$y = \frac{3x}{4} + c$$

$$y = \frac{3x + 4c}{4}$$

$$4y = 3x + 4c$$

$$\underline{3x - 4y + 4c = 0}$$

STEP 3 :

$$d = 4$$

$$\left| \frac{3(-2) - 4(1) + 4c}{\sqrt{3^2 + 4^2}} \right| = 4$$

$$\left| \frac{-6 - 4 + 4c}{5} \right| = 4$$

$$\left| \frac{-10 + 4c}{5} \right| = 4$$

$$\frac{-10 + 4c}{5} = \pm 4$$

$$-10 + 4c = \pm 20$$

$$-10 + 4c = 20 \quad \left| \quad -10 + 4c = -20 \right.$$

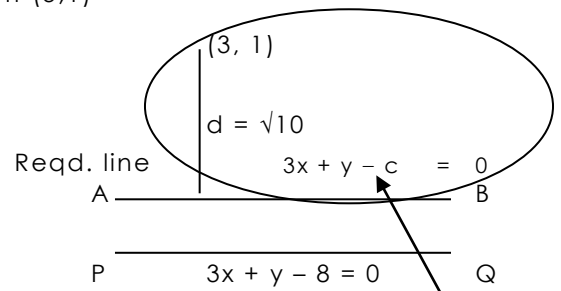
$$4c = 30 \quad \left| \quad 4c = -10 \right.$$

$$\text{Equation of AB} \quad \left| \quad \text{Equation of AB} \right.$$

$$\underline{3x - 4y + 30 = 0} \quad \left| \quad \underline{3x - 4y - 10 = 0} \right.$$

03.

Find equation of line parallel to $3x + y - 8 = 0$ and which is at a distance of $\sqrt{10}$ units from the point $(3, 1)$



STEP 1 : PQ

$$3x + y - 8 = 0 \quad m = \frac{-a}{b} = \frac{-3}{1} = -3$$

STEP 2 : AB

$$m_{AB} = -3 \quad (AB \parallel PQ)$$

$$\text{equation of AB : } y = mx + c$$

$$y = -3x + c$$

$$\underline{3x + y - c = 0}$$

STEP 3 :

$$d = \sqrt{10}$$

$$\left| \frac{3(3) + (1) - c}{\sqrt{3^2 + 1^2}} \right| = \sqrt{10}$$

$$\left| \frac{9 + 1 - c}{\sqrt{10}} \right| = \sqrt{10}$$

$$\left| \frac{10 - c}{\sqrt{10}} \right| = \sqrt{10}$$

$$\frac{10 - c}{\sqrt{10}} = \pm \sqrt{10}$$

$$10 - c = \pm 10$$

$$10 - c = 10 \quad \left| \quad 10 - c = -10 \right.$$

$$-c = 0 \quad \left| \quad -c = -20 \right.$$

$$c = 0 \quad \left| \quad c = 20 \right.$$

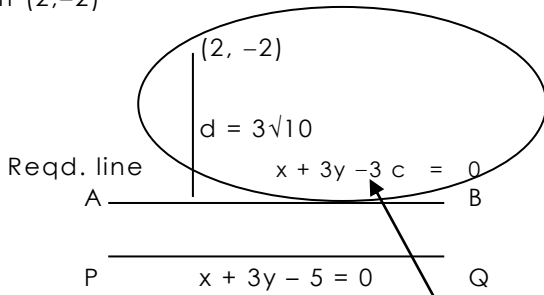
$$\text{Equation of AB} \quad \left| \quad \text{Equation of AB} \right.$$

$$\underline{3x + y = 0} \quad \left| \quad \underline{3x + y - 20 = 0} \right.$$

SOLUTION - QSET 5B

04.

Find equation of line parallel to $x + 3y - 5 = 0$ and which is at a distance of $3\sqrt{10}$ units from the point $(2, -2)$



STEP 1 : PQ

$$x + 3y - 5 = 0 \quad m = \frac{-a}{b} = \frac{-1}{3}$$

STEP 2 : AB

$$m_{AB} = -1/3 \text{ (AB//PQ)}$$

$$\text{equation of AB : } y = mx + c$$

$$y = \frac{-1x}{3} + c$$

$$3y = -x + 3c$$

$$\underline{x + 3y - 3c = 0}$$

STEP 3 :

$$d = 3$$

$$\left| \frac{(2) + 3(-2) - 3c}{\sqrt{1^2 + 3^2}} \right| = 3\sqrt{10}$$

$$\left| \frac{2 - 6 - 3c}{\sqrt{10}} \right| = 3\sqrt{10}$$

$$\left| \frac{-4 - 3c}{\sqrt{10}} \right| = 3\sqrt{10}$$

$$\frac{-4 - 3c}{\sqrt{10}} = \pm 3\sqrt{10}$$

$$-4 - 3c = \pm 30$$

$$-4 - 3c = 30 \quad | \quad -4 - 3c = -30$$

$$-3c = 34 \quad | \quad -3c = -26$$

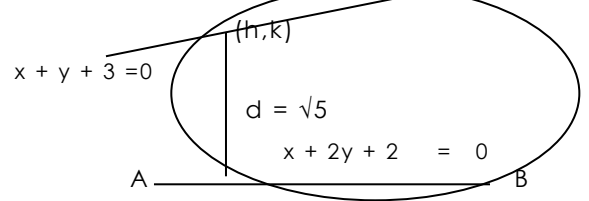
$$3c = -34 \quad | \quad 3c = 26$$

$$\text{Equation of AB} \quad | \quad \text{Equation of AB}$$

$$\underline{x + 3y + 34 = 0} \quad | \quad \underline{x + 3y - 26 = 0}$$

01.

Find the points on the line $x + y + 3 = 0$ whose distance from $x + 2y + 2 = 0$ is $\sqrt{5}$ units



STEP 1 :

Since (h, k) lies on $x + y + 3 = 0$, it must satisfy the equation

$$\therefore h + k = -3 \dots\dots (1)$$

STEP 2 :

$$d = \sqrt{5}$$

$$\left| \frac{h + 2k + 2}{\sqrt{1^2 + 2^2}} \right| = \sqrt{5}$$

$$\frac{h + 2k + 2}{\sqrt{5}} = \pm \sqrt{5}$$

$$h + 2k + 2 = \pm 5$$

$$h + 2k + 2 = 5$$

$$h + 2k = 3 \dots (2)$$

Solving (1) & (2)

$$h + k = -3$$

$$- \frac{h + 2k}{1} = -3$$

$$-k = -6$$

$$k = 6$$

$$h + 6 = -3$$

$$h = -9$$

$$(-9, 6)$$

$$h + 2k + 2 = -5$$

$$h + 2k = -7 \dots (3)$$

Solving (1) & (3)

$$h + k = -3$$

$$- \frac{h + 2k}{1} = -7$$

$$-k = 4$$

$$k = -4$$

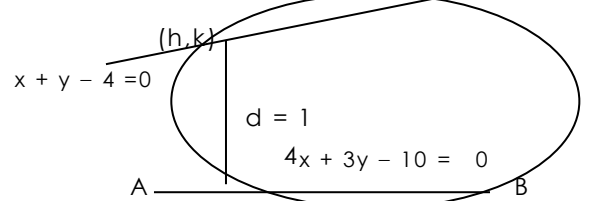
$$h - 4 = -3$$

$$h = 1$$

$$(1, -4)$$

02.

Find the points on the line $x + y - 4 = 0$ whose distance from $4x + 3y = 10$ is 1 units



STEP 1 :

Since (h,k) lies on $x + y - 4 = 0$, it must satisfy the equation

$$\therefore h + k = 4 \dots\dots (1)$$

STEP 2 :

$$d = 1$$

$$\left| \frac{4h + 3k - 10}{\sqrt{4^2 + 3^2}} \right| = 1$$

$$\frac{4h + 3k - 10}{5} = \pm 1$$

$$4h + 3k - 10 = \pm 5$$

$$4h + 3k - 10 = 5 \quad | \quad 4h + 3k - 10 = -5$$

$$4h + 3k = 15 \dots\dots (2) \quad | \quad 4h + 3k = 5 \dots\dots (3)$$

Solving (1) & (2)

Eq (1) x 4

$$\begin{array}{r} 4h + 4k = 16 \\ -4h + 3k = -15 \\ \hline k = 1 \end{array}$$

subs in (1)

$$\begin{array}{r} h + 1 = 4 \\ h = 3 \\ (3, 1) \end{array}$$

Solving (1) & (3)

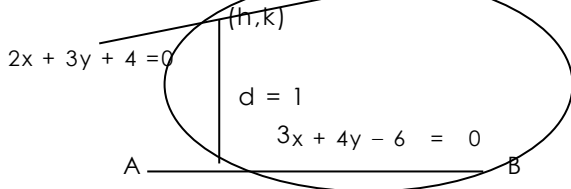
Eq (1) x 4

$$\begin{array}{r} 4h + 4k = 16 \\ -4h + 3k = -5 \\ \hline k = 11 \end{array}$$

$$\begin{array}{r} h + 11 = 4 \\ h = -7 \\ (-7, 11) \end{array}$$

03.

Find the points on the line $2x + 3y + 4 = 0$ whose distance from $3x + 4y - 6 = 0$ is 2 units



STEP 1 :

Since (h,k) lies on $2x + 3y + 4 = 0$, it must satisfy the equation

$$\therefore 2h + 3k = -4 \dots\dots (1)$$

STEP 2 :

$$d = 1$$

$$\left| \frac{3h + 4k - 6}{\sqrt{3^2 + 4^2}} \right| = 2$$

$$\frac{3h + 4k - 6}{5} = \pm 2$$

$$3h + 4k - 6 = \pm 10$$

$$3h + 4k - 6 = 10 \quad | \quad 3h + 4k - 6 = -10$$

$$3h + 4k = 16 \dots\dots (2) \quad | \quad 3h + 4k = -4 \dots\dots (3)$$

Solving (1) & (2)

$$2h + 3k = -4 \quad \times 3$$

$$3h + 4k = 16 \quad \times 2$$

$$\begin{array}{r} 6h + 9k = -12 \\ -6h + 8k = -32 \\ \hline k = -44 \end{array}$$

subs in (1)

$$2h + 3(-44) = -4$$

$$2h - 132 = -4$$

$$2h = -4 + 132$$

$$2h = 128$$

$$h = 64$$

$$(64, -44)$$

Solving (1) & (3)

$$2h + 3k = -4 \quad \times 3$$

$$3h + 4k = -4 \quad \times 2$$

$$\begin{array}{r} 6h + 9k = -12 \\ -6h + 8k = 8 \\ \hline k = -4 \end{array}$$

subs in (1)

$$2h + 3(-4) = -4$$

$$2h - 12 = -4$$

$$2h = -4 + 12$$

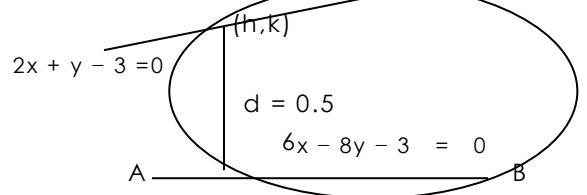
$$2h = 8$$

$$h = 4$$

$$(4, -4)$$

04.

Find the points on the line $2x + y - 3 = 0$ whose distance from $6x - 8y - 3 = 0$ is 0.5 units



STEP 1 :

Since (h,k) lies on $2x + y - 3 = 0$, it must satisfy the equation

$$\therefore 2h + k = 3 \dots\dots (1)$$

STEP 2 :

$$d = 0.5$$

$$\left| \frac{6h - 8k - 3}{\sqrt{6^2 + 8^2}} \right| = 0.5$$

$$\frac{6h - 8k - 3}{10} = \pm 0.5$$

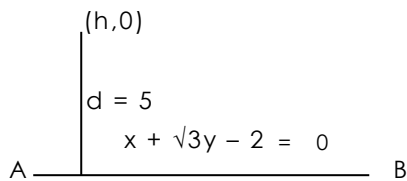
$$6h - 8k - 3 = \pm 5$$

$6h - 8k - 3 = 5$ $6h - 8k = 8$ $3h - 4k = 4 \dots (2)$ <p>Solving (1) & (2)</p> $2h + k = 3 \quad \times 4$ $3h - 4k = 4$ $8h + 4k = 12$ $3h - 4k = 4$ <hr style="width: 100%;"/> $11h = 16$ $h = \frac{16}{11}$ <p>subs in (1)</p> $\frac{32}{11} + k = 3$ $k = 3 - \frac{32}{11}$ $k = \frac{1}{11}$ <p>$(\frac{16}{11}, \frac{1}{11})$</p>	$6h - 8k - 3 = -5$ $6h - 8k = -2$ $3h - 4k = -1 \dots (3)$ <p>Solving (1) & (3)</p> $2h + k = 3 \quad \times 4$ $3h - 4k = -1$ $8h + 4k = 12$ $3h - 4k = -1$ <hr style="width: 100%;"/> $11h = 11$ $h = 1$ <p>subs in (1)</p> $2 + k = 3$ $k = 1$ <p>$(1, 1)$</p>
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05.

Find the coordinates of the point on X - axis whose distance from the line $x + \sqrt{3}y - 2 = 0$ is

5 units



STEP 1 :

$$d = 5$$

$$\left| \frac{h + \sqrt{3}(0) - 2}{\sqrt{1^2 + \sqrt{3}^2}} \right| = 5$$

$$\frac{h - 2}{2} = \pm 5$$

$$h - 2 = \pm 10$$

$h - 2 = 10$ $h = 12$ $(12, 0)$	$h - 2 = -10$ $h = -8$ $(-8, 0)$
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